

# Local Uncertainty Benchmarking

## *A coal case study*

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# Acronyms

**SMU** -> Selective mining unit

(the smallest volume used for ore/waste delineation)

**CS** -> Conditional Simulations

**DHSA** -> Drill Hole Spacing Analysis (global)



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# Local uncertainty

## Why is it important?

- Kriged estimate -> block scale ( $\cong$ drill hole spacing)
- But short term mining decisions based on SMU scale
- Variability,  $\sigma_{SMU} \gg \sigma_{Block}$
- Penalty elements, ore specification, delivery contracts
- Need to understand local uncertainty
  - > at smaller than drill hole spacing -> at SMU scale
- Investigate shorter term uncertainty
- > integrate method into mine planning and operational decisions



At the SMU scale

*Can relative uncertainty be approximated by co-kriging?*



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# Key project objectives

- #1** Investigate feasibility of using SMU kriging variances
- #2** Develop and validate a relative simple methodology to
  - provide timely local uncertainties on SMUs
  - be implemented on site
- #3** Use stringent benchmarking to
  - validate results
  - support and defend proposed methodology



# Methodology

ST = seam thickness

Var<sub>ACC</sub> = Accumulated Variable, eg. Ash<sub>ACC</sub> = ASH x ST

P5 = 5<sup>th</sup> percentile

	Co-Kriging	Conditional co-simulations
1		Clean data set - ST and Var <sub>ACC</sub> Calculate residuals
2		Gaussian Anamorphosis of data
3	Cross-variography	Cross-variography of Gaussian variables
4	Co-Krige ST, Var <sub>ACC</sub> into SMUs	Co-simulate Gaussian variables (1000 realisations) Back-transform to ST*, Var <sub>ACC</sub> *
5		Add global drift trend to each estimate
6		Ash* = Ash <sub>ACC</sub> * / ST*
7	St. Dev of Ash*	Average point values in each CS realisation into SMUs
8	P5, P95 ≈ Ash* ± 1.645*St Dev	P5, P95 extracted from simulations 90% CI = [P5,P95]



# Results

- Thickness, Fluorine, Phos closest to normally distributed
- Ash – peaked distributions (higher kurtosis)
- Sulphur – right skewed
- Benchmark uncertainty estimates will typically have 4.6% sampling uncertainty
- 90%CI
- Relative uncertainty =  $\frac{90\% \text{ CI}}{\text{estimated SMU value}}$

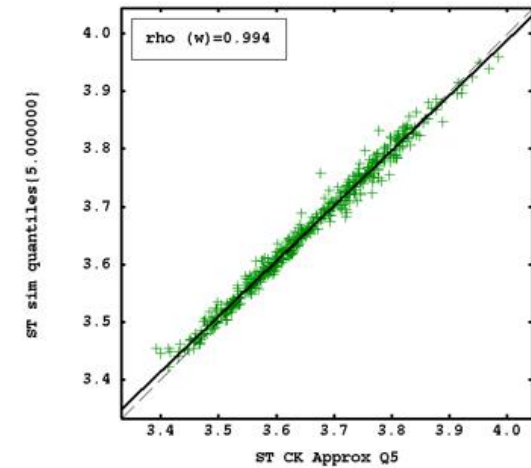


# Results

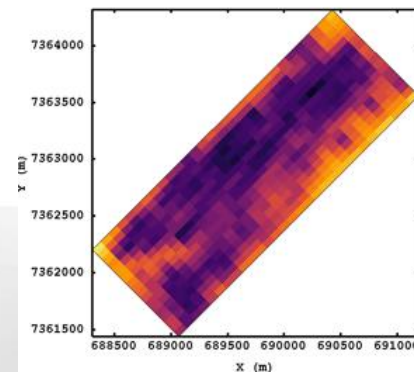
## Relative uncertainty for Conditional Simulations and Co-Kriging

Variable	CS	CoK
Thickness	5.0%	5.2%
Ash	11.8%	14.7%
Fluorine	45.6%	40.8%
Phos	35.8%	37.3%
Sulphur	35.8%	37.3%

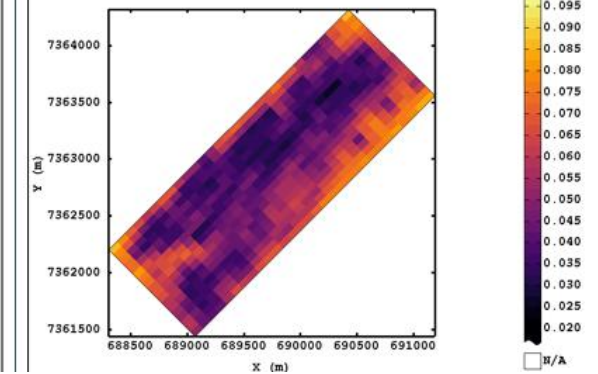
ST Q5 simulation v (Co-)Kriging



ST (Co-)Kriging rel. uncertainty



ST simulation rel. uncertainty

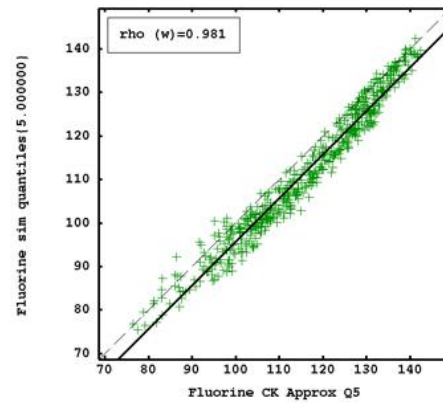


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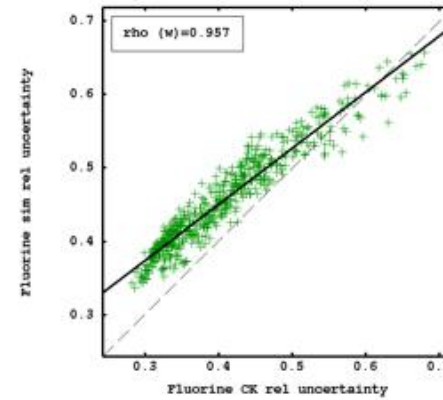


# Results

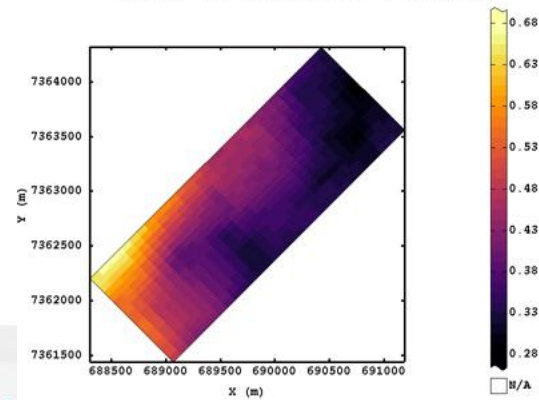
Fluorine Q5 simulation v (Co-)Kriging



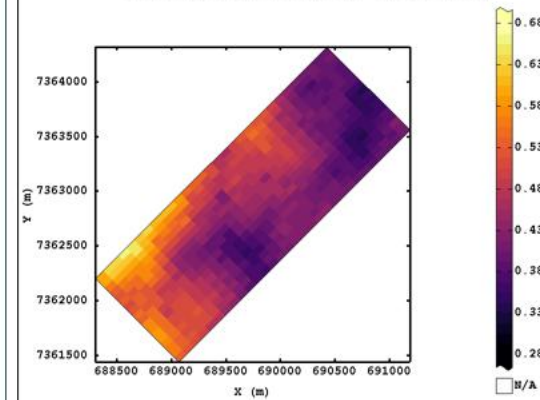
Fluorine rel. uncertainty simulation v (Co-)Kriging



Fluorine (Co-)Kriging rel. uncertainty



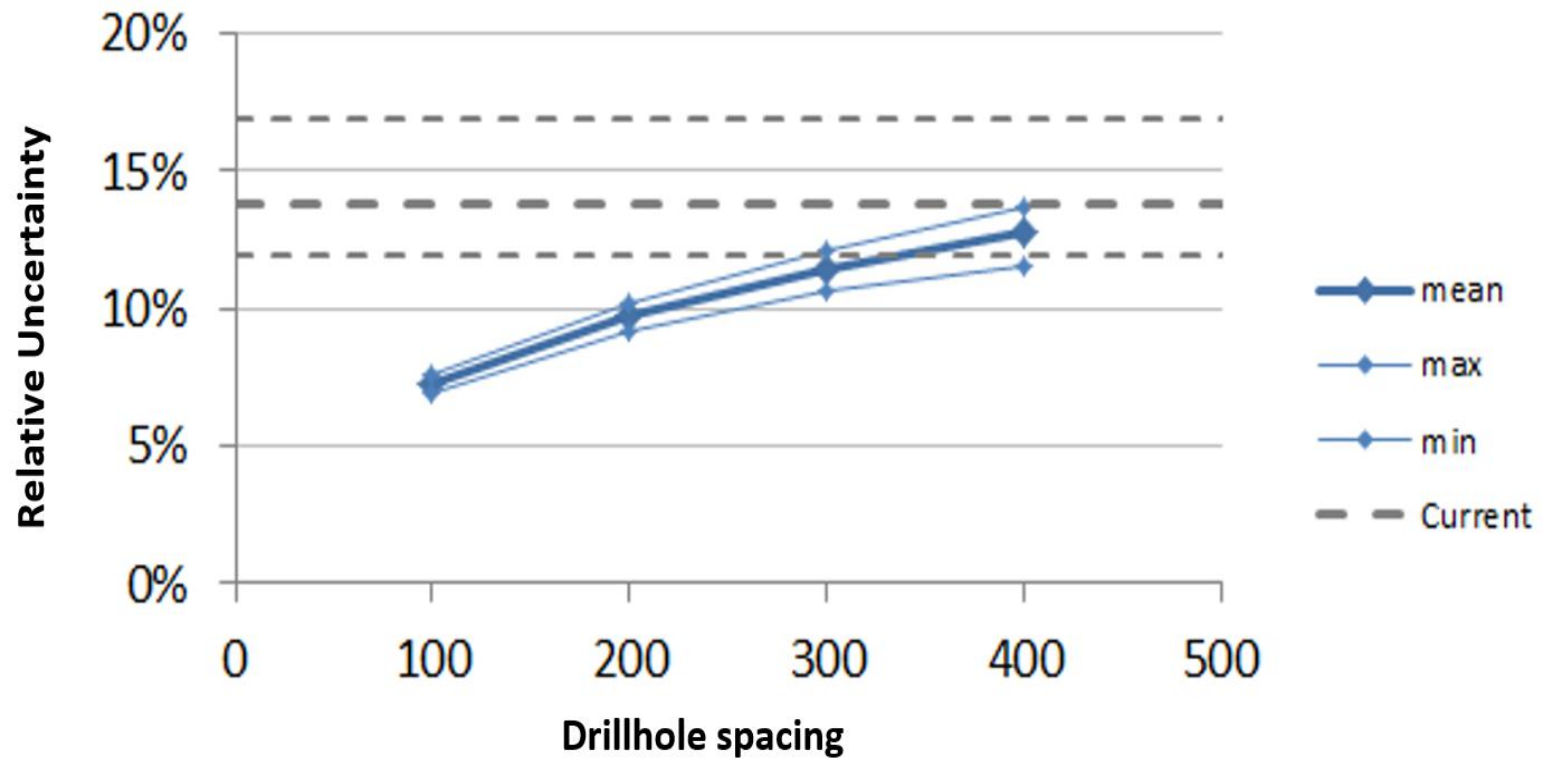
Fluorine simulation rel. uncertainty



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# Results

Relative uncertainties (90%CI) by SMU



# Conclusions

- Agreement between kriged and simulation methods is
  - Excellent for thickness
  - Very reasonable for quality variables
- CS benchmarking supports use of Co-kriging variances to estimate SMU uncertainties.

In hard rock mining using CS for local uncertainty estimates is certainly more common than in coal. However, definitely not mainstream yet. DHSA gives first pass answer so there is a potential to extend this coal, 2D case study into 3D, non coal applications. *Bearing in mind, it is only the first pass application.*



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My co-authors and I wish to thank Geovariances and BHP for their support in presenting this work.

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